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User-Extensible Sequences in Common Lisp

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ABSTRACT
Common Lisp is often touted as the programmable programming language, yet it sometimes places large barriers in the way, with the best of intentions. One of those barriers is a limit to the extensibility by the user of certain core language constructs, such as the ability to define subclasses of built-in classes usable with standard functions: even where this could be achievable with minimal penalties. We introduce the notion of user-extensible sequences, describing a protocol which implementations of such classes should follow. We show examples of their use, and discuss the issues observed in providing support for this protocol in a Common Lisp, including ensuring that there is no performance impact from its inclusion.

1. INTRODUCTION
Common Lisp is recognized as being an extremely flexible language: one in which linguistic experimentation can take place, one where the method of solving a problem in a domain is first to write an interpreter or a compiler for a language to express concepts in the domain of interest, and then to use that domain-specific language to solve the problem. To some extent, then, it might be surprising to find some of the ways in which extension of Common Lisp (by the implementor or user) is limited. This is at least partially explained by the aims of the standardizers, which included “stricter standardization for portability” (Pitman and Chapman 1994 section 1.1.2): codification of existing practice was a large part of the X3J13 committee’s work, and it is difficult to ensure portability with a highly-extensible language core.

However, the standardization process was not intended to close the door to language development: merely to provide a stable platform which could be agreed on. For example, the CLOS system for object orientation was standardized without very much scope for extensibility; however, it was intentionally (Steele 1990 chapter 28) upwardly compatible with something close to the Metaobject Protocol described in Kiczales et al. 1991, often (though not always) supported by contemporary Lisp implementations.

Meanwhile, other languages and language environments have not stood still; many of Lisp’s once-unique features are now to be found in other languages (Norvig 2002), though some are still not\(^1\) additionally, sometimes these languages have features not found in any available Lisp implementation. In some cases, such as Aspect-Oriented Programming (Kiczales et al. 1997) these features can be straightforwardly implemented by any interested user — this itself is one of Lisp’s unique features not often found elsewhere — but some features need implementation support for them to be used to maximum effect: addition of features by the Lisp programmer can suffice for certain needs, but they are not pervasive in the way that one would want; such extensions, even upwardly-compatible extensions, need to be explicitly used by third-party code.

One such extension is the ability for the user to define new sequence types. For the purposes of this paper, a sequence is a finite ordered collection; more concretely, a sequence has a number of elements, addressable by an integer between 0 (inclusive) and the sequence’s length (exclusive). The motivation for allowing the definition of new sequence types is primarily to eliminate the need for new names for essentially the same concept: examples of such from real-world code include climacs-buffer:size and flexichain:nb-elements (Strandh et al. 2004) as analogues for length on user-defined data structures, and tabcode-syntax:buffer-position-if (Rhodes et al. 2005) for position-if; these multiple names are a barrier to clear expression and understanding of Common Lisp code which defines objects which are conceptually sequences. Additionally, the implementation of sequence functionality is tedious and error-prone\(^2\) and it is more convenient to require of the datastructure implementor only a few simple method definitions to achieve all the standard sequence functionality.

We describe in this paper a proposal for implementations to allow users to define new sequence classes which interoperate seamlessly with the standard Common Lisp sequence functions. The basic mode of operation of our design is as

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1 and it has been argued that their inclusion would convert their host language into a Lisp of some form.

2 The author, in developing this extension, wrote the implementation first and test cases second: the test cases revealed five implementation errors.
We wish to make defining new sequence classes simple and convenient for users, so that simply defining a subclass of sequence and a few methods specialized on that class suffices for the entire sequence functionality to be available, and also to provide enough hooks for sequence class implementors to be able to customize the behaviour for their own needs.

- We wish not to overly constrain implementations of this protocol, allowing implementors to make trade-offs to reflect the needs of their users. In particular, we wish to allow both a simple implementation (where the Common Lisp implementation supports this protocol natively for all sequence types) and an implementation where existing code suffers no run-time performance penalty; additionally, we do not wish to render a portable implementation impossible, though we believe that such an implementation would necessarily have visible seams.

While it is possible to recommend ways of accessing and iterating over both Common Lisp sequences and other objects in userspace, there is no way of having those other objects (conceptually sequences though not of type sequence) seamlessly interoperate with the standard Common Lisp sequence functionality, or with third-party code which does not follow such a recommendation.

The desire not to constrain implementations of this proposal leads to the creation of a new package name to name the operators providing the extensible functionality, allowing dispatch from the standard function to the extensible one through trampolining or defadvice-like mechanisms. However, an implementation of Common Lisp wishing to support this proposal natively may choose to implement some of its CL symbols as direct imports from the new sequence package.

In what follows, there will be reference to new operators without explicit package prefixes: in such cases, the symbols’ package should be assumed to be the sequence package. A number of new operators have the same name as standardized operators of Common Lisp; except in appendix A the operator without an explicit prefix should be taken to mean the Common Lisp operator, while the new operators will have an explicit sequence: prefix.

1.2 Compatibility

The types [sic] vector and the type list are disjoint subtypes of type sequence, but are not necessarily an exhaustive partition of sequence.

Although the quote above might suggest that there would be no problem from the point of view of formal standard con-

Figure 1: How to detect formally nonconforming implementations of [make-sequence] If calling foo with any argument causes the type-error handler to be called, the Common Lisp implementation is, strictly speaking, nonconforming.

The rest of this paper is organized as follows: we introduce the design considerations of this proposal in section 1.1; then, after discussing compatibility issues and related work in sections 1.2 and 1.3, we give an introduction for the prospective user of extensible sequences in section 2, and some examples in section 3, and some details of our implementation are given in section 4. As a snapshot of our work in progress, a more formal specification of the protocols is presented in appendix A, intended in the first instance to stimulate discussion rather than to be the definitive specification.

1.1 Design considerations

Our design for this extension as a whole was influenced by a number of desiderata:

- We wish to minimize incompatibility with the existing Common Lisp standard, introducing such incompatibility only where strictly necessary. There are only a few corner cases where the existing standard document needs to be clarified or reinterpreted; see section 1.2 for discussion of this point.

- We wish to make defining new sequence classes simple and convenient for users, so that simply defining a subclass of sequence and a few methods specialized on that class suffices for the entire sequence functionality to be available, and also to provide enough hooks for sequence class implementors to be able to customize the behaviour for their own needs.

- We wish not to overly constrain implementations of this protocol, allowing implementors to make trade-offs to reflect the needs of their users. In particular, we wish to allow both a simple implementation (where
Table 1: The protocol functions which must be implemented for a sequence class. Three correspond directly to primitive sequence operations in Common Lisp; adjust-sequence and make-sequence-like provide support for components of higher-level destructive and consing operations respectively (see Table 2).

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>sequence:length</td>
<td>Return the length of a sequence.</td>
</tr>
<tr>
<td>sequence:elt</td>
<td>Return the element at a given index.</td>
</tr>
<tr>
<td>(setf sequence:elt)</td>
<td>Set the element at a given index.</td>
</tr>
<tr>
<td>sequence:adjust-sequence</td>
<td>Adjust the sequence.</td>
</tr>
<tr>
<td>sequence:make-sequence-like</td>
<td>Make a new sequence.</td>
</tr>
</tbody>
</table>

Performance for an implementation to offer non-standard types of [sequence](#) the outline code in figure 1 as a result of Issue **CONCATENATE-SEQUENCE** (Pitman 1990b), defined by ANSI CL never to get a type-error branch of the **handler-case** which was probably not intended by the standardizers. For a fuller discussion of this issue, and a suggestion for a resolution, see Rhodes (2006).

An additional issue with formal compliance is that ANSI CL specifies for the [length](#) function and the [elt](#) accessor that their sequence argument should be a **proper sequence**, which is defined in the normative glossary as a **sequence which is not an improper list; that is, a vector or a proper list**; again, this definition was probably not intended to prohibit non-standardized sequences, even though, interpreted strictly, the second half of it implies that no non-standard sequence is a proper sequence.

We must also consider the issue of cultural compatibility with the body of Common Lisp code available in the wild. Perhaps because of the historical lack of generic sequences offered by Common Lisp implementations, there seems to be little in the way of packages written to exploit the abstract sequence data type; instead, packages choose a concrete sequence type and implement their functionality atop that, manipulating a particular kind of sequence rather than sequences in general. However, it is likely that if user-extensible sequences become available, code will be modified or written afresh to take advantage of it.

It would be possible to implement this proposal (or something like it) entirely portably in ‘userspace’, by defining a new package shadowing many of the standard Common Lisp functions and macros, and implementing the generic functionality on the standard types by trampolining to the Lisp functions and macros, and implementing the generic abstract sequence data type; instead, packages choose a concrete sequence type and implement their functionality atop that, manipulating a particular kind of sequence rather than sequences in general. However, such an implementation strategy has drawbacks:

- Implementation-specific compiler optimizations (such as compiler macros) for the shadowed functions would essentially be lost. As an example, if an implementation has a specialized implementation of [map-into](#) for arguments known at compile-time to be certain types of vector, that optimization will go unused in a putative userspace implementation in function calls to sequence-cl:map-into.
- The userspace implementation of extensible sequences would not interoperate with third-party Common Lisp code: programs already written with generic (not necessarily user-extensible) sequences in mind, using the common-lisp package, will not be able to interoperate cleanly with sequences defined using this portable implementation.
- Innocuous-looking uses of explicit package prefixes (for example, cl:sequence) would have surprising and potentially difficult-to-debug effects. Other maintenance headaches include how to support both native and portable implementations in library code.

A userspace implementation might be better than nothing, for a transition period, but support from the Lisp implementation is required for seamless operation.

That said, there is an issue regarding portability of libraries using extensible sequences: until it is ubiquitously implemented, use of this facility in bodies of code render those bodies of code unportable in practice. Whether this unportability itself becomes a problem in practice is largely a matter for the user community to decide.

### 1.3 Related Work

Much inspiration for this proposal was drawn from the Dylan [Shalit 1996](#) iterator protocol, which provides for iteration over collections with the open generic function **forward-iteration-protocol**. Where our design is similar to this protocol, it is largely for the same reasons: we do not wish to impose unnecessary run-time overhead (in space or speed) for those uses which need high performance. However, in this proposal, we aim to provide a little more of a layer of convenience for the user who does not need to minimize overhead.

Many other languages provide some form of iteration or collection protocol. Python, for instance, allows the implementation of a collection to define a method on __iter__() to return an iterator object, which itself must have methods on __iter__() and next(). Apparently for reasons of efficiency, the Python iterator protocol (Yee and van Rossum 2001) provides no explicit means for checking for termination of an iteration, instead requiring the iterator to signal an exception when next() is called on an iterator representing a terminated iteration.

The Scheme language (Kelsey et al. 1998) definition has little built-in support for user-extensible or even generic sequences. Its community has made one attempt (Miller 2004) at defining an interface and conventions for collections; however, this SRFI has apparently not seen many Scheme implementations decide to support it natively; as of two years after its finalization, the SRFI status page reports no implementation as supporting it.
The Factor language’s sequence interface is conceptually very similar to that described in the following sections for Common Lisp, including the distinction between sequence protocol (defining the fundamental operations that must be implemented for sequence objects) and ‘utility words’, analogous to functions performing computations over sequences (Pestov 2006) Sequences), which will work on any object implementing the sequence protocol.

In the Common Lisp world itself, an early (pre-CLOS) attempt to provide generic sequence functionality was presented in Haible (1988) for the GNU CLISP implementation; however, that proposal was never formally exported or documented (Haible 2006); the author’s primary concern with this attempt was in supporting the necessary operations efficiently. Some of these issues of efficiency remain in this proposal, though we believe that they might be resolved in a Lisp implementation supporting sealing and inlining of methods.

2. USER-DEFINED SEQUENCES

In this section, we must draw the distinction between the implementor of a sequence class, and the implementation of Common Lisp which supports this user-extensible sequence facility. Most of the time, we will use ‘user’ to mean the implementor of a sequence class, and ‘implementor’ to mean implementor of a Common Lisp implementation, and we hope that it will be clear from context when this does not apply.

The names of the various operators have been chosen to maximize both backward- and forward-compatibility (with Common Lisp as standardized, and with potential related extensions to Common Lisp such as a collections protocol); we specify operators corresponding to standardized functions such as find to be named like sequence:find, so that an implementation of Common Lisp ‘natively’ implementing this proposal can simply import the relevant symbols from the sequence package. Thus, we specify sequence:adjust-

sequence rather than (setf sequence:length), so that an implementation can import sequence:length into the standard common-lisp package without inadvertently causing there to be a setf function for length, in contravention of the constraints on implementations [Pitman and Chapman 1994 Section 11.1.2.1.1).

We also aim to be not incompatible with similar extensions to Common Lisp, such as a protocol for accessing and iterating over general collections; in this proposal we are dealing with user-defined sequence classes because Common Lisp as standardized has a large library of functions acting on generic sequences, while it has no functions acting on generic collections – and so a ‘userspace’ implementation of a collections protocol would not pose the interoperability problems discussed in section 1.2.

2.1 Sequence Datatypes

Under this proposal, the user may define a direct subclass of sequence using defclass specifying sequenced as one of the superclasses (but not the only one: for code portable between implementations of this proposal, standard-object must be in the superclasses list too). The resulting class is subtypep sequence, and instances of the class are typep sequence.

The fundamental operations defined in Common Lisp relating to sequences are length elt and (setf elt); in order to support these, the user of the extensible sequence facility (the implementor of the sequence class) should define methods on sequence:length, sequence:elt and (setf sequence:elt).

Implementation may not simply make sequence a nickname for the common-lisp package, as the list of package nicknames is standardized as c1 only.

Reviewers of this paper have raised concerns about the use of sequence as a direct superclass, suggesting instead a protocol class, maybe sequence-object, as the user-specializable class. The author wishes to acknowledge reviewer concerns in this matter, while continuing to present the protocol as currently implemented.

<table>
<thead>
<tr>
<th>Common Lisp Function</th>
<th>Extensible Generic Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>copy-seq</td>
<td>sequence:copy-seq</td>
</tr>
<tr>
<td>reduce-fill</td>
<td>sequence:reduce, sequence:fill</td>
</tr>
<tr>
<td>reverse</td>
<td>sequence:reverse</td>
</tr>
<tr>
<td>sort</td>
<td>sequence:sort</td>
</tr>
<tr>
<td>count</td>
<td>sequence:count</td>
</tr>
<tr>
<td>find</td>
<td>sequence:find</td>
</tr>
<tr>
<td>count-if</td>
<td>sequence:count-if</td>
</tr>
<tr>
<td>find-if</td>
<td>sequence:find-if</td>
</tr>
<tr>
<td>position</td>
<td>sequence:position</td>
</tr>
<tr>
<td>position-if</td>
<td>sequence:position-if</td>
</tr>
<tr>
<td>position-if-not</td>
<td>sequence:position-if-not</td>
</tr>
<tr>
<td>search</td>
<td>sequence:search</td>
</tr>
<tr>
<td>mismatch</td>
<td>sequence:mismatch</td>
</tr>
<tr>
<td>replace</td>
<td>sequence:replace</td>
</tr>
<tr>
<td>substitute</td>
<td>sequence:substitute</td>
</tr>
<tr>
<td>naSubstitute</td>
<td>sequence:naSubstitute</td>
</tr>
<tr>
<td>substitute-if</td>
<td>sequence:substitute-if</td>
</tr>
<tr>
<td>substitute-if-not</td>
<td>sequence:substitute-if-not</td>
</tr>
<tr>
<td>remove</td>
<td>sequence:remove</td>
</tr>
<tr>
<td>delete</td>
<td>sequence:delete</td>
</tr>
<tr>
<td>remove-if</td>
<td>sequence:remove-if</td>
</tr>
<tr>
<td>delete-if</td>
<td>sequence:delete-if</td>
</tr>
<tr>
<td>remove-duplicates</td>
<td>sequence:remove-duplicates</td>
</tr>
<tr>
<td>delete-duplicates</td>
<td>sequence:delete-duplicates</td>
</tr>
</tbody>
</table>

Table 2: Common Lisp functions, and the corresponding generic functions specified to be extensible in this protocol. Calling the Common Lisp function with an extended sequence as an argument will cause applicative methods on the extensible generic function to be invoked; whether this is achieved through defadvice, trampolining or function identity is left unspecified.
The set of functions making up the sequence protocol of this proposal (see table 1) consists of the analogues to the three Common Lisp functions above, along with two others: sequence:adjust-sequence, which is similar to the adjust-array function, but generalized to sequences; and sequence:make-sequence-like, which creates a sequence of the the same kind as its first argument, with length given by its second argument.

The rationale for make-sequence-like is to support the subseq and copy-seq operators, and the sequence functions which are defined to return a freshly-arsed sequence (such as substitute). Additionally, this operator is easier both to specify and to implement efficiently than one like the make-sequence function, which requires a full understanding of the Common Lisp type system; make-sequence-like can operate as a simple generic function specialized on its sequence argument.

To support the delete and delete-duplicates functions, we provide adjust-sequence, which adjusts various properties, including the length, of a sequence. Users of this protocol are encouraged to document the circumstances under which their methods on this operator will preserve the identity of its sequence argument, and must arrange that if a new sequence is allocated, the original sequence argument must not be modified; however, in general, callers (either explicit or implicit) may not assume that the sequence returned from adjust-sequence is the same sequence as its argument.

Once methods for these generic functions have been implemented for a sequence class, all the regular Common Lisp sequence functionality will work as expected. However, some sequences may not admit implementations of all these operations, or indeed might offer means to implement certain operations more efficiently, so in the following sections we describe the protocol by which the Lisp implementation provides the sequence functionality.

2.2 Iteration

It is common to iterate over sequences, both in the conception of many of the Common Lisp sequence functions, and in user-defined operations. In this section, we describe the protocol and interface for iterating over sequence contents, both built-in and user-defined. The protocol discussed here has a set of default methods specialized on the sequence class, so that any sequence class for which methods on the protocol functions of section 2.1 have been implemented will obey the protocol. However, these default methods cannot take into account the characteristics of any particular sequence class, and so for efficiency users may wish to override them for their own classes.

The essential concept is the use of an iterator object to represent the current state of an iteration. It is not necessary for this iterator object to have a distinguished class, as the sequence over which it is iterating is present in all function calls in this protocol (and therefore its class can be used for specialization of methods); indeed, the conceptual object is represented in this protocol by three objects and six functions. This iteration protocol is close to the one available in Dylan (Shalit 1996).

The make-sequence-iterator operator constructs one of these iterator objects: after the required sequence argument, it accepts keyword :start, :end and :from-end arguments, and returns nine values. The first three of those values are an iterator state, a limit and the from-end argument; the remaining six are functions which, respectively, return a state one step ahead, if possible; test the state against the limit for termination; retrieve the element at the current iteration state from the sequence; set the element at the current iteration state to a new value; return the index corresponding to the current iteration state; and return a distinct iteration state representing a copy of the current one.

The default method on make-sequence-iterator is intended for convenience: for most uses, it is unnecessary to construct the nine return values; instead, the default method (specialized to sequence) on make-sequence-iterator generates the first three of the return values by calling make-simple-sequence-iterator, and returns in addition six protocol generic functions: #'iterator-step (which advances the iteration state); #'iterator-endp, testing an iteration for termination; the #'iterator-element reader and the #'(setf iterator-element) writer; #'iterator-index, returning the sequence index corresponding to the iterator state; and finally #'iterator-copy, returning a copy of the iteration state. These functions have methods specialized to list and vector to provide iterators for the built-in sequence classes.

While implementors of sequence classes may choose to use this CLOS-based iterator protocol (at the potential loss of efficiency through generic function dispatch at each step), users of the iteration protocol (who define functions which perform iterations over sequences) may not assume that the sequence class implementor has done so, and so must call make-sequence-iterator or the operators discussed below.

A small dose of syntactic sugar around make-sequence-iterator is provided by with-sequence-iterator, which binds as if by multiple-value-bind the variables in its first argument to the result of applying make-sequence-iterator to its second argument, and then executes the body. A slightly simpler macro to use is with-sequence-iterator-functions, which binds the six names in its first argument to six local functions (which have dynamic extent and close over the return values from make-sequence-iterator) which perform the various iterator manipulations.

For programmer convenience, we also provide a dosequence macro, behaving as dolist (but for arbitrary sequences), and an extension for loop using the loop keywords element and elements, in a similar fashion to the for-as-package loop path (Pitman and Chapman 1994 Section 6.1.2.1.7).

It is intended that the iteration protocol described here will be compatible with an iteration protocol for general collections (including hash tables, trees and other similar data structures); at the minimum, any such protocol should be
Table 3: Common Lisp functions applicable or otherwise relevant to sequences which are not specified as extensible in this protocol; however, the implementation’s versions are specified to be applicable to arbitrary sequence types, and to produce the expected result.

<table>
<thead>
<tr>
<th>some</th>
<th>every</th>
<th>notany</th>
</tr>
</thead>
<tbody>
<tr>
<td>notevery</td>
<td>map</td>
<td>map-into</td>
</tr>
<tr>
<td>concatenate</td>
<td>merge</td>
<td>make-sequence</td>
</tr>
</tbody>
</table>

2.3 Sequence Functions

For most of the functions in the sequences chapter of the standard, there is an analogous generic function with the same argument list which can be specialized for user-defined sequence classes. The complete list of generic functions specified to be extensible, and their corresponding Common Lisp function, is given in table 2. Implementations of this proposal may choose to make the Common Lisp function eq to the extensible generic function, or even make the symbols themselves eq to each other; however, users may not assume this.

2.4 Other Affected Functions

The Common Lisp functions in table 3 are not extensible in this proposal. We discuss the interaction of this proposal with the behaviour of those functions below; in summary, where ANSI CL specifies that they accept sequence arguments, the implementation must accept any user-defined sequence, and where ANSI CL specifies that they accept a sequence type-specifier, they must accept a user-defined sequence name or class object (see also Rhodes (2006) for a discussion of the implications of this with respect to the standard behaviour).

Six functions in the SEQUENCES chapter of the ANSI CL standard do not have the structure for user-extensibility in the same straightforward way as the functions discussed in section 2.3; they are concatenate, map, merge, make-sequence, coerce, and map-into.

Taking map-into first, we simply specify that an implementation of user-extensible sequences must implement the map-into function such that target sequences and source sequences of arbitrary subtype of sequence are supported given a complete implementation of the sequence and iteration protocol of sections 2.1 and 2.2. An implementation is not prohibited from providing a means of customizing the behaviour of map-into but neither is it required to.

A means of extending the behaviour of concatenate, map, merge, make-sequence, and coerce is likewise left unspecified, though again an implementation of this document must provide for the functionality of these functions to be available for objects of arbitrary sequence type and type specifiers naming a concrete subtype of sequence for details of how this interacts with the ANSI CL specified behaviour of these functions, see Rhodes (2006). It is likely that any documented fashion of extending these five functions will use the same mechanism for all of them.

As for functions which are not in the SEQUENCES chapter of the ANSI CL specification, the intent is that where a particular behaviour is specified for a sequence argument, that behaviour should be implemented for the user-extensible sequences. For instance, the short-circuiting quantifiers some, every, not everybody, and not any should accept sequence arguments of arbitrary class; make-array’s initial-contents argument (and the #a array reader) should accept a sequence of sequences, as specified, including user-extensible sequences. Note that we do not specify a different behaviour of the equal function from the standard-mandated one (of using eq on objects of type standard-object); although equal is specified to descend arrays and conses, it does not do so in a sequence-like way, and in particular a list and a vector with the same content are not considered to be equal. Equality over sequence contents can be computed with mismatch.

Particular attention must be paid to the read-sequence and write-sequence functions. Although Gray (1989) does not suggest that these functions be extensible in the manner of the other stream functions, it is likely that this is because read-sequence and write-sequence were added to the language after the extensible streams proposal was made, and indeed Common Lisp implementations have provided stream-read-sequence and stream-write-sequence generic functions for user customizability. Lisps providing both an implementation of this proposal and extensible streams based on Gray (1989) should document the effect of calling stream-read-sequence and stream-write-sequence with arguments being instances of non-standardized classes. The simple-streams (Franz Inc. 2006) Chapter 83) extensible analogue is documented to signal an error for all sequence types other than strings and octet vectors; if this restriction is relaxed, there are similar interactions as with Gray streams over which extensibility (sequence or stream) takes precedence.

3. EXAMPLES

In this section, we present two examples of uses for the protocols discussed in this paper. Firstly, in section 3.1 we present the implementation of a distinct sequence type along with the method definitions to allow it to interoperate; then, in section 3.2 we demonstrate the definition of a mixin class and methods specialized on it to provide additional functionality to generic sequences implemented as in this paper.

3.1 Queue

As an example of a non-standard sequence, consider implementing a queue data structure, which supports the operations enqueue and dequeue. Figure 2 shows one way in which such a queue could be implemented, using a list as the storage for the data, and keeping a reference to the cons cell at the back of the queue. Purely for interest, we also implement a variant of the queue which is also funccallable, and arrange so that calling the funccallable queue with no arguments performs dequeueing, while with one argument it queues that argument.

An implementation of the sequence and iteration protocol
(defclass queue (sequence standard-object)
  ((%data :accessor %queue-data) (%pointer :accessor %queue-pointer)))
(defmethod initialize-instance :after ((o queue) &key)
  (let ((head (list nil)))
    (setf (%queue-data o) head (%queue-pointer o) head)))

(defun enqueue (data queue)
  (:argument-precedence-order queue data)
  (:method (data (o queue))
    (setf (cdr (%queue-pointer o)) (list data) (%queue-pointer o) (cdr (%queue-pointer o)))
    o))

(defun dequeue (queue)
  (:method ((o queue))
    (prog1 (cadr (%queue-data o))
      (setf (cdr (%queue-data o)) (cddr (%queue-data o)))))

(defun length (o queue))
  (length (cdr (%queue-data o))))
(defun elt (o queue) index)
  (elt (cdr (%queue-data o)) index)
(defun (setf elt) (new-value (o queue) index)
  (setf (elt (cdr (%queue-data o)) index) new-value)
(defun make-sequence-like (o queue length &key (initial-element nil iep) (initial-contents nil icp))
  (let ((result (make-instance (class-of o))))
    (cond
      ((and iep icp)
        (error "supplied both ~S and ~S to " :initial-element :initial-contents 'make-sequence-like))
      (icp (unless (= (length initial-contents) length)
        (error "length mismatch in ~S" 'make-sequence-like))
        (setf (cdr (%queue-data result)) (coerce initial-contents 'list)
          (%queue-pointer result) (last (%queue-data result))))
      (t (setf (cdr (%queue-data result)) (make-list length :initial-element initial-element)
          (%queue-pointer result) (last (%queue-data result))))
    result)))
(defun adjust-sequence (o queue length &key initial-element (initial-contents nil icp))
  (cond
    ((= length 0)
      (setf (cdr (%queue-data o)) nil (%queue-pointer o) (%queue-data o)))
    (t (sequence:adjust-sequence (%queue-data o) (1+ length) :initial-element initial-element)
      (setf (%queue-pointer o) (last (%queue-data o)))
      (when icp (replace (%queue-data o) initial-contents :start1 1))
    ))

(defun make-simple-sequence-iterator ((q queue) &rest args &key from-end start end)
  (declare (ignore from-end start end))
  (apply #'sequence:make-simple-sequence-iterator (cdr (%queue-data q)) args))
(defmethod iterator-step ((q queue) iterator from-end)
  (sequence:iterator-step (cdr (%queue-data q)) iterator from-end)
  (sequence:iterator-endp (cdr (%queue-data q)) iterator from-end)
  (sequence:iterator-element (cdr (%queue-data q)) iterator)
  (sequence:iterator-index (cdr (%queue-data q)) iterator))
(defmethod iterator-copy ((q queue))
  (sequence:iterator-copy (cdr (%queue-data q)))
  (sequence:iterator-copy (cdr (%queue-data q)))

Figure 2: Basic definitions of a queue data structure, including a funcallable variant. The layout of the code in this and subsequent figures is not idiomatic for reasons of space.

Figure 3: Implementation of the sequence protocol for the queues of figure 2. The first five method definitions are sufficient to allow all sequence functionality to run correctly; the methods on the iterator functions reduce the complexity for our simple queue implementation from $O(N^2)$ to $O(N)$ for most operations.
We assume for expository purposes that the destructive
native strategy for grouping multiple primitive operations,
used in the method for recording calls to `msubstitute` and
`delete` is shown in figure 6 in the appendix.

4. IMPLEMENTATION DETAILS

We have implemented the above proposal in Steel Bank
Common Lisp (Newman et al., 2000); the overall strategy
was to modify the implementations of the standard Common
Lisp sequence functions to call into their `sequence` package
analogues instead of signalling an error; if their sequence
arguments were neither lists nor vectors. This way of im-
plementing this proposal was motivated by changing the
run-time performance characteristics of the system as little
as possible for existing code.

The first aspect of SBCL itself which needed to be modified
was the type system: the system needed to be informed that
`sequence` was no longer simply an alias in that implementa-
tion of `(or list vector)`, but was an unsealed (that is,
subclassable) class with its own identity in the type system;
since the SBCL compiler makes heavy use of type inference,
both when compiling user code and when cross-compiling it-
self, it was also important for the compiler’s version of sub-
typep to know that the types `(and sequence vector)` and
`(and sequence list)` are equivalent to `vector` and `list`
respectively, irrespective of the extensibility of `sequence`.

Additionally, the declared return type of various sequence
functions such as `copy-seq` needed to be altered: SBCL
has the type `consed-sequence`, which was previously aliased
to `(or list (simple-array * (*)))`, expressing that (in SBCL)
freshly consed vectors do not have fill-pointers, are not
displaced and are not adjustable. In an implementa-
tion supporting extensible sequences, this type alias needs to
be changed to `(or (simple-array * (*)) (and sequence
(not vector)))` to correctly represent the implementation’s
behaviour.

After these modifications to the type system, the implemen-
tation of the remainder of this proposal involved two distinct
parts: modifying SBCL itself to insert calls to the sequence
generic functions (say, `sequence:length`) from the standard
functions (`length`), and implementing those generic func-
tions in a userspace library. Incremental development of the
SBCL internals was eased by the use of a `seq-dispatch`
macro, taking a sequence argument and expanding into ei-
thewo or three cases: one for when the argument is a list,
one when it is a vector, and (optionally) one for neither:
the third case is only executed when a generic sequence is
encountered.

The various compiler transformations and optimizations of
sequence functions such as `find position map coerce`
were largely unaffected, as either the various checks on their
applicability were already restrictive enough, or else the op-
timizations performed were generic to all sequences. The
implementation of `find position` and `find position` (and `if`
and `if`-relatives) needed a small amount of alteration to allow
sequence functions such as `reverse` act in-place on the user-
extended sequences in which this class will be mixed.

SBCL has a sophisticated understanding of the Common
Lisp type system, so such complex types do not cause diffi-
culty in type inference.
(defclass undoable-mixin ()
  ((recording :initform nil :accessor recording) (record :initform nil :accessor record)))
(defclass setelt-record ()
  ((index :initarg :index :reader index) (value :initarg :value :reader value)))
(defclass fill-record ()
  ((start :initarg :start :reader start) (end :initarg :end :reader end)
   (contents :initarg :contents :reader contents)))
(defclass nreverse-record ()
  ((recording :initform nil :accessor recording) (record :initform nil :accessor record)))
(defmacro without-undoing ((object) &body body)
  "(let ((old (recording ,object)))
    (unwind-protect (progn (setf (recording ,object) t) ,@body)
      (setf (recording ,object) old))))
(defmacro define-undo-method (name arglist &body body)
  '(
    (defmethod ,name :around ,(substitute '(o undoable-mixin) 'o arglist)
      (if (recording o) (call-next-method) (without-undoing (o) ,@body (call-next-method))))
    (defmethod undo-undoing-record ((o undoable-mixin) (r null)) (error "Nothing to undo")
      (defmethod undo-undoing-record ((o undoable-mixin) r) (pop (record o)))
    (defmethod undo-undoing-record :after ((o undoable-mixin) r (setelt-record))
      (push (make-instance 'setelt-record :index index :value (elt o index)) (record o)))
    (defmethod undo-undoing-record ((o undoable-mixin) (r nreverse-record))
      (defmethod undo-undoing-record ((o undoable-mixin) (r fill-record))
        (with-accessors ((start start) (end end) (contents contents)) r (setf (subseq o start end) contents)))
      (undo-using-record object (car (record object)))
      (undo-using-record ((recording :initform nil :accessor recording) (record :initform nil :accessor record)))
      (undo-using-record ((index :initarg :index :reader index) (value :initarg :value :reader value)))
    (undo-using-record ((o undoable-mixin) (r null)) (error "Nothing to undo")
      (undo-using-record ((o undoable-mixin) (r setelt-record))
        (undo-using-record ((o undoable-mixin) (r fill-record))
          (undo-using-record ((o undoable-mixin) (r nreverse-record)))
          (without-undoing (o) (setf (subseq o start end) contents))))
    (defmethod undo-undoing-record ((o undoable-mixin) r nreverse-record))
    (without-undoing (o) (sequence:nreverse o))))

Figure 5: Illustration of a simple implementation of undo for sequences: an undoable-mixin class which can be mixed in to a sequence class, providing undo functionality (illustrated here for (setf elt), fill and nreverse).

the protocol for sequence:find and sequence:position described in section A.3 to be implemented, while the implementation of map was improved in the process of development, being rewritten to use dynamic-extent support, resolving a long-standing issue in the system.

Support for defining subclasses of sequence from the customized PCL [Bobrow and Kiczales 1988] which SBCL incorporates to implement CLOS was as simple as modifying the system method for the MetaObject Protocol function mop:validate-superclass to allow sequence as a direct superclass of classes with metaclasses standard-class and mop:functional-standard-class. In addition, to support the operations involving sequence type specifiers (such as map and merge), we used make-sequence-like acting on the mop:class-prototype of the class named by the type specifier, if that class was a subclass of sequence.

SBCL’s loop facility is based on the MIT implementation, so it was straightforwardly extended using the add-loop-path operator as shown in figure 6.

In the implementation of this proposal for SBCL, there is no run-time performance impact for bodies of code which does not use the facilities provided by user-extensible sequences (see http://sbcl.boinkor.net/bench/ for benchmark data: the relevant changeset is labelled 1.0.0.22). This is understandable, as all that has been done to the runtime code in this implementation is to convert cases which used to signal errors (usually the type-error for the datum not being a sequence) into calls to the analogous function of the sequence package. Changes in compile-time performance are potentially present but unmeasurable: the only likely contributor is the additional work in computing type relationships between sequence and other types. There is an increase of approximately 1% of the heap size of a fresh SBCL instance, because of the extra code used in implementing this proposal; however, this extra space is in a tenured generation and behind a write barrier, and therefore does not significantly increase garbage-collection times.

5. CONCLUSIONS

We have described an extension to Common Lisp to allow users to define their own sequence classes in an interoperable manner, and have described the changes necessary to implement this extension in a contemporary implementation. Additionally, we have attempted to justify the need for this extension in terms of expressivity and parsimony, and given simple examples of using it.

We leave for future work the related task of defining a protocol for user-defined collections; Common Lisp sequences are a specialized form of collection, finite and ordered. However, preliminary work suggests that such a collection protocol can be defined to interoperate with the proposals in this document for sequences.

It is intended that a revised and expanded version of appendix A should be submitted to some suitable forum for standardization of some form; it is likely that feedback gath-
(defun loop-elements-iteration-path (variable data-type prep-phrases)
  (let (of-phrase)
    (loop for (prep . rest) in prep-phrases do
      (ecase prep
        ((:of :in) (if of-phrase
                    (sb-loop::loop-error "Too many prepositions")
                    (setq of-phrase rest)))
      (destructuring-bind (it lim f-e step endp elt seq)
        (loop repeat 7 collect (gensym)
          (push '(let ((,seq ,(car of-phrase)))) sb-loop::*loop-wrappers*)
          (push '(sequence:with-sequence-iterator (,it ,lim ,f-e ,step ,endp ,elt) (,seq)) sb-loop::*loop-wrappers*)
          …)
        (sb-loop::add-loop-path
          '(element elements) 'loop-elements-iteration-path sb-loop::*loop-ansi-universe*
          :preposition-groups '((:of :in)) :inclusive-permitted nil))

Figure 6: Extension of \texttt{loop} for a loop path to iterate over the elements of generic sequences.

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APPENDIX
A. SPECIFICATION
In the sections below, all of the generic functions and macros being specified are named by symbols external in the \textit{sequence} package. In cases where the generic function being defined corresponds to a standardized Common Lisp function, it is not specified whether the corresponding Common Lisp function is distinct from the specified...
Figure 7: Implementation of reader macros and print functions for queues and funcallable queues. Note the support for correct behaviour in the presence of non-nil values of printer control variables.

generic functions, nor indeed whether the symbol in the common-lisp package is distinct from that in the sequence package; that is, #\'length might or might not be eql to #\'sequence:length, and length might or might not be eql to sequence:length. The sequence package may have additional, implementation-specific names; sequence need not be the package-name of the package.

It is not specified whether the methods specified on list and vector are in fact called when the Common Lisp function corresponding to the generic function is called on such data. It is not specified whether the methods specified on sequence are called when the Common Lisp function corresponding to the generic function is called on data of type vector or list.

In implementations which support the Metaobject Protocol as defined in Kiczales et al. (1991), suitable methods on mop:validate-superclass should be provided such that no error is signalled for user-defined sequence classes of metaclass standard-class, such implementations are additionally encouraged to allow mop:funcallable-standard-class as a compatible metaclass for user-defined sequence classes.

A.1 Basic sequence operations

We specify generic functions length, elt and (setq elt) to correspond to the Common Lisp functions with the same name. In each case, there are two primary methods with the sequence argument specialized on list and on vector, providing the standard-defined behaviour for the Common Lisp operator, and a third method with the sequence argument specialized on sequence which signals an error of type type-error for compatibility with the standard requirement of the sequence argument to be a proper sequence.

In addition, we specify two new generic functions and corresponding methods (with a similar pattern of behaviour) described below.

Generic Function make-sequence-like

Syntax:
make-sequence-like sequence length &key initial-element initial-contents

This generic function returns a sequence of the same class as its sequence argument, with the specified length. If neither initial-element nor initial-contents is supplied, the consequences are undefined if any element of the resulting sequence is read before being written. If initial-element is provided, it is used to initialize the resulting sequence; if initial-contents is provided, it must be a sequence of length length, which is used to initialize the resulting sequence. The consequences are undefined if both initial-element and initial-contents are supplied.

Primary Method make-sequence-like (l list) length &key initial-element initial-contents

No behaviour for these methods is specified beyond that for the generic function.

Primary Method make-sequence-like (v vector) length &key initial-element initial-contents

This method signals an error of type type-error

Generic Function adjust-sequence

Syntax:
adjust-sequence sequence length &key initial-element initial-contents
(defmethod sequence:make-sequence-iterator :around ((o undoable-mixin) &key from-end start end)
  (declare (ignore from-end start end))
  (multiple-value-bind (s l f step endp elt setelt index copy) (call-next-method)
    (lambda (nv s i)
      (if (recording s)
        (funcall setelt nv s i)
        (without-undoing (s)
          (push (make-instance 'setelt-record :index (funcall index s i) :value (funcall elt s i))
            (record s))
          (funcall setelt nv s i)))))

(defmacro with-compound-recording ((object) &body body)
  '(let ((old (recording ,object)) (or (record ,object)))
    (unwind-protect
      (progn (setf (recording ,object) nil) (setf (record ,object) nil) ,@body)
        (setf (recording ,object) old)
        (setf (record ,object) (cons (make-instance 'compound-record :records (record ,object)) or)))))

(defclass compound-record () ((records :initarg :records :reader records))))

(defmethod undo-using-record ((o undoable-mixin) (r compound-record))
  (dolist (r (records r)) (undo-using-record o r)))

(defmacro define-compound-undo-method (name arglist)
  '(define-undo-method ,name ,arglist
    (with-compound-recording (o) (call-next-method))))

(define-compound-undo-method sequence:nsubstitute (new old o &key from-end start end test test-not key count))
(define-compound-undo-method sequence:nsubstitute-if (new old o &key from-end start end key count))
(define-compound-undo-method sequence:nsubstitute-if-not (new old o &key from-end start end key count))

(define-compound-undo-method sequence:delete (item o &key from-end (start 0) end test test-not key count))
(define-compound-undo-method sequence:delete-if (item o &key from-end (start 0) end key count))
(define-compound-undo-method sequence:delete-if-not (item o &key from-end (start 0) end key count))
(define-compound-undo-method sequence:delete-duplicates (o &key from-end (start 0) end test test-not key))
(define-compound-undo-method sequence:replace (o sequence2 &key (start1 0) end1 (start2 0) end2)
  (push (make-instance 'fill-record :start start1 :end end1 :contents (coerce (subseq o start1 end1) 'vector))
    (record o)))

(define-compound-undo-method sequence:sort (o predicate &key key)
  (push (make-instance 'fill-record :contents (coerce o 'vector) :start 0 :end nil) (record o)))

Figure 8: Implementation details of the undoable mixin. The setter in the iterator protocol is wrapped by
the :around method on make-sequence-iterator; a specialized undo record is defined for adjust-sequence; and undo records for
nsubstitute and delete are represented as sequences of primitive undo records, treated as
an atom for the purposes of running undo.)
This generic function changes the length or elements of sequence. It returns a sequence of length length, with contents as specified by initial-contents if provided, otherwise with the original contents in their original position and initial-element as any additional elements. The return value may, but need not, share structure with or be identical to the sequence argument.

**Primary Method** adjust-sequence (l list) length &key initial-element initial-contents

**Primary Method** adjust-sequence (v vector) length &key initial-element initial-contents

This method functions in a similar manner to adjust-array though the implementation may choose to preserve the identity of the argument if it has a fill pointer and the length argument is not greater than the size of the vector.

**Primary Method** adjust-sequence (s sequence) length &key initial-element initial-contents

This method signals an error of type type-error.

### A.2 Iteration

**Generic Function** make-sequence-iterator

Syntax:

```
make-sequence-iterator sequence &key from-end start end
```

This generic function returns nine values: three values corresponding to an iterator state, a limit state and from-end, and six functions with signatures and functionality like the iterator- functions below.

**Primary Method** make-sequence-iterator (s sequence) &key from-end (start 0) end

This method returns the three values returned by calling make-simple-sequence-iterator, along with the iterator functions #'iterator-step, #'iterator-endp, #'iterator-element, #'setf iterator-element, #'iterator-index and #'iterator-copy defined below.

For the seven following generic functions, we describe both the generic function and also in more detail the return values of the primary method, specialized on sequence. The primary methods described here are suitable for iteration across data structures with efficient random access, such as vectors, and less suitable for iteration across some other data structures, such as lists. We expect implementations of this protocol to provide additional methods to perform more efficient iteration on lists than is possible with the primary method described; however, we do not impose additional requirements on the behaviour of such methods.

**Generic Function** make-simple-sequence-iterator

Syntax:

```
make-simple-sequence-iterator sequence &key from-end start end
```

This generic function returns three values: an iterator object, a limit state and from-end. These values, along with sequence, are to be used for calling to the iterator generic functions, below; the consequences are unspecified if objects not returned by a call to make-simple-sequence-iterator are passed as arguments to the iterator functions. The primary method returns the three values start, end (or the length of sequence if end is false) and nil if from-end is false; if from-end is true, it returns the three values (1- (or end (length sequence))), (1- start), and from-end.

**Generic Function** iterator-step

Syntax:

```
iterator-step sequence iterator from-end
```

This generic function returns a new iterator state representing the advancement of the iteration across sequence in the direction indicated by from-end. The primary method returns (1- iterator) if from-end is true; otherwise, it returns (1+ iterator).

**Generic Function** iterator-endp

Syntax:

```
iterator-endp sequence iterator limit from-end
```

This generic function tests the iterator for having reached its end state for iteration across sequence indicated in the direction indicated by from-end. The primary method returns the value of (= iterator limit).

**Generic Function** iterator-element

Syntax:

```
iterator-element sequence iterator
```

This generic function returns the element of sequence at the point of iteration indicated by iterator. The primary method returns the value of (elt s iterator).

**Generic Function** (setf iterator-element)

Syntax:

```
(setf iterator-element) new-value sequence iterator
```

This generic function sets the element of sequence at the point of iteration indicated by iterator to new-value. The primary method returns the value of (setf (elt s iterator) new-value).

**Generic Function** iterator-index

Syntax:

```
iterator-index sequence iterator
```

This generic function returns the index of the point indicated by iterator in sequence. The primary method returns iterator.

**Generic Function** iterator-copy

Syntax:

```
iterator-copy sequence iterator
```

This generic function returns an iterator state identifying the same point in an iteration as iterator, such that changes to one do not affect the other. The primary method returns iterator.

**Macro** with-sequence-iterator (&optional state limit from-end step endp elt setelt index copy) (sequence &key from-end (start 0) end) &body body
This macro binds the names in its first argument list as if by \texttt{multiple-value-bind} to the values returned by \texttt{make-sequence-iterator} applied to its second argument list, and then executes \texttt{body}.

\textit{Macro} \texttt{dosequence} (var sequence-form \&optional result-form) \&body body

This macro iterates over a sequence, in a similar fashion to \texttt{dolist} iterating over a list. The \texttt{body} is like a \texttt{tagbody} consisting of a series of tags and statements.

\texttt{dosequence} evaluates \textit{sequence-form}, which should produce a sequence. It then executes the \texttt{body} once for each element in the sequence, in the order in which the tags and statements occur, with \texttt{var} bound to the element. Then \textit{result-form} is evaluated with \texttt{var} bound to \texttt{nil}.

An implicit block named \texttt{nil} surrounds the entire \texttt{dosequence} form. \texttt{return} may be used to terminate the loop immediately without performing any further iterations, returning zero or more values.

The scope of the binding of \texttt{var} does not include the \textit{sequence-form}, but the \textit{result-form} is included.

It is implementation-dependent whether \texttt{dosequence} establishes a new binding of \texttt{var} on each iteration or whether it establishes a binding for \texttt{var} once at the beginning and then assigns it on any subsequent iterations.

\textit{Loop Path} \texttt{for-as-sequence}

This allows using an iteration variable, as with other loop \texttt{for-as-} clauses, as if the following clause were added to the \texttt{loop} grammar [Pitman and Chapman 1994. Macro \texttt{Loop}):

\begin{verbatim}
for-as-sequence::=
  var [type-spec] being {each | the}
  {element | elements} {in | of} sequence
\end{verbatim}

and as if the \texttt{for-as-subclause} clause permitted this \texttt{for-as-sequence} clause along with the standardized clauses. As with other iteration control clauses, the variable argument may be a destructuring list. The effect of this clause is to iterate through the contents of a sequence, starting from the zeroth element and terminating at the end of the sequence\footnote{Note that this behaviour is different from that of the \texttt{for-as-across} loop clause on vectors with fill pointers.}.

It is unspecified whether the generic functions specified below are called when the corresponding Common Lisp function has only \texttt{list} and \texttt{vector} arguments for sequences; however, the implementation is required to provide methods for these generic functions implementing similar behaviour, so that the user may call these generic functions on \texttt{list} and \texttt{vector} sequences.

For each Common Lisp function in table 2 we specify a generic function of the same name in the \texttt{sequence} package with the same argument list, each with a default method where all sequence arguments are specialized on \texttt{sequence}.

Given that the sequence argument to these functions is named \texttt{sequence}, we enumerate the specified calling relationships between these functions as follows:

\begin{itemize}
  \item the default method on \texttt{copy-seq} calls \texttt{subseq} with parameters \texttt{sequence} and 0;
  \item the default method on \texttt{substitute} calls \texttt{copy-seq} on \texttt{sequence}, and then calls \texttt{nsubstitute} on its arguments with the provided sequence replaced by the copy. This pattern is repeated for the \texttt{-if} and \texttt{-if-not} variants of \texttt{substitute}, and for \texttt{remove}, \texttt{remove-if}, \texttt{remove-if-not} and \texttt{remove_duplicates} calling the corresponding \texttt{delete-} function.
  \item the default method on \texttt{sort} behaves as if it constructs a vector with the same elements as \texttt{sequence}, calls \texttt{sort} on that vector, then replaces the elements of \texttt{sequence} with the elements of the sorted vector.
\end{itemize}

The rationale behind specifying these calling relationships is to make clear the work needed by a sequence class implementor to install specialized implementations of these functions for particular sequence classes.

\vspace{1cm}

\section*{A.3 Sequence Function Specifications}

Except as specified here, it is implementation-dependent whether methods on these generic functions call other such generic functions or not. For each of these generic functions there is a method, called the “default method” below, where all sequence parameters are specialized on \texttt{sequence} implementing the default behaviour given an implementation of the iteration and basic sequence protocol in the sections above. The user of this protocol is permitted to extend or override these generic functions, but is not permitted to specialize any non-sequence argument.

\footnote{Note that this behaviour is different from that of the \texttt{for-as-across} loop clause on vectors with fill pointers.}